# Core Mathematics C3 Advanced Level 

For Edexcel

Paper G<br>Time: 1 hour 30 minutes

Instructions and Information
Candidates may use any calculator EXCEPT those with the facility for symbolic algebra, differentiation and/or integration.
Full marks may be obtained for answers to ALL questions.
The booklet 'Mathematical Formulae and Statistical Tables', available from Edexcel, may be used.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Advice to Candidates

You must show sufficient working to make your methods clear to an examiner. Answers without working may gain no credit.

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1. The third and fifth terms of an arithmetic progression are $\ln 18$ and $\ln 162$ respectively.

Find (a) the exact value of the common difference,
(b) the first term.
2. Express

$$
\frac{2 x+5}{4 x^{2}-9} \times \frac{2 x^{2}-x-3}{2(x+1)}
$$

as a single fraction in its simplest form.
3. The function f is defined by and the function $g$ is defined by
(a) What is the range of $\mathrm{f}(x)$ ?
f: $x \mapsto \cos x, \quad 0 \leq x \leq \pi$,
$\mathrm{g}: x \mapsto x+\frac{\pi}{2}, \quad x \geq 0$.
(b) What is the domain of $\operatorname{fg}(x)$ ?
(c) What is the range of $\operatorname{fg}(x)$ ?
4. (a) Given that $\sin x=\frac{7}{25}$ and that the angle $x$ is obtuse,
find the exact value $\sin 2 x$.
(b) Prove that $\tan \left(\frac{\pi}{4}-\theta\right)=\frac{1-\tan \theta}{1+\tan \theta}$.
5. The function f is even and has a domain $\mathbb{R}$.

$$
\begin{array}{lll} 
& \mathrm{f}(x)=a-x, & \text { for } \\
\text { and } \quad & 0 \leq x \leq a \\
\mathrm{f}(x)=2 x-2 a, & \text { for } & x>a,
\end{array}
$$

where $a$ is a positive constant
(a) Sketch the curve with equation $y=\mathrm{f}(x)$ showing the coordinates of all the points at which the curve meets the axes.
(b) Find, in terms of $a$, the values of $\mathrm{f}(2 a)$ and $\mathrm{f}(-2 a)$.
(c) Find the values of $x$ for which $\mathrm{f}(x)=\frac{1}{2} a$.
6. Show that

$$
y=\mathrm{e}^{2 x}(\cos 3 x+\sin 3 x)
$$

satisfies the equation $\frac{\mathrm{d}^{2} y}{\mathrm{~d} x^{2}}-4 \frac{\mathrm{~d} y}{\mathrm{~d} x}+13 y=0$.
7. The curve $C$ has the equation $y=\mathrm{f}(x)$, where

$$
\mathrm{f}(x)=4 x-\ln x, \quad x>0
$$

The point $A$ is a stationary point on $C$.
(a) Calculate the coordinates of $A$ and determine the nature of the stationary point.
$B$ is the point on the curve $C$ whose $x$ coordinate is 1 .
(b) Find the equations of both the tangent and normal to the curve at the point $B$.

The tangent at $B$ meets the $x$-axis at $P$, and the normal at $B$ meets the $x$-axis at $Q$.
(c) Find the area of the $\triangle P B Q$.
8. (a) Given $\mathrm{f}(x)=5 \sin x+12 \cos x$,
find $\mathrm{f}(x)$ in the form $R \sin (x+\alpha)$ where $R$ and $\alpha$ are positive constants to be found. ( $0<\alpha<90^{\circ}$ )

Hence or otherwise find,
(b) the minimum value of $\mathrm{f}(x)+4$,
(c) the smallest positive value of $x$ for which this minimum value occurs,
(d) the values of $x, 0<x<360^{\circ}$, which satisfy the equation

$$
\begin{equation*}
5 \sin x+12 \cos x=6 \tag{5}
\end{equation*}
$$

